

$$\begin{aligned}
 4m - 2p &= 0; & \left(\frac{1}{3}, \frac{2}{3}\right) \\
 -3m + 9p &= 5
 \end{aligned}$$

$$\begin{aligned}
 4m - 2p &= 0 & -3\left(\frac{1}{3}p\right) + 9p &= 5 & 4m - 2\left(\frac{2}{3}\right) &= 0 \\
 \frac{4m}{4} &= \frac{2p}{4} & -3p + 9p &= 5 & 4m - \frac{4}{3} &= 0 \\
 m &= \frac{1}{2}p & \frac{6p}{1} &= 5 & 4m &= \frac{4}{3} \\
 & & \frac{15}{3}p &= \frac{5}{1} & m &= \frac{1}{3} \\
 & & p &= \frac{1}{3} & &
 \end{aligned}$$

Solve the following systems using any method you choose:

1)  $\begin{cases} 2x + 3y = 4 \\ 3x - 4y = 7 \end{cases}$

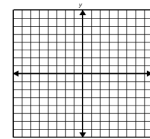
2)  $\begin{cases} x + y = -12 \\ 2x - 3y = 6 \end{cases}$

3)  $\begin{cases} 5x - 2y = 3 \\ 2x - y = 0 \end{cases}$

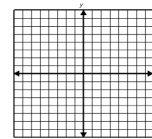
4)  $\begin{cases} 5x - 7y = 2 \\ 3x = 4y \end{cases}$

Graph the following inequalities:

5)  $y - 2x \leq 1$



6)  $-2y + 6x < 2$



6)  $-2y + 6x < 2$

$$\begin{aligned}
 -2y + 6x &< 2 \\
 -6x &-6x \\
 \hline
 -2y &< -6x + 2 \\
 \frac{-2y}{-2} &< \frac{-6x + 2}{-2} \\
 y &> 3x - 1
 \end{aligned}$$

5)  $y - 2x \leq 1$

$$\begin{aligned}
 y - 2x &\leq 1 \\
 +2x &+2x \\
 \hline
 y &\leq 2x + 1
 \end{aligned}$$

$$4) \begin{cases} 5x - 7y = 2 \\ 3x = 4y \end{cases} \quad (-8, -6)$$

$$\begin{array}{r|l} \begin{array}{l} 5x - 7y = 2 \\ 3x - 4y = 0 \end{array} & \begin{array}{l} 3(-8) = 4y \\ -24 = 4y \\ y = -6 \end{array} \\ \hline \begin{array}{l} 20x - 28y = 8 \\ -21x + 28y = 0 \end{array} & \begin{array}{l} -x = 8 \\ x = -8 \end{array} \end{array}$$

$$3) \begin{cases} 5x - 2y = 3 \\ 2x - y = 0 \end{cases} \quad (3, 6)$$

$$\begin{array}{r|l} \begin{array}{l} 5x - 2y = 3 \\ 10x - 4y = 6 \end{array} & \begin{array}{l} 2x - 6 = 0 \\ 2x = 6 \\ x = 3 \end{array} \\ \hline \begin{array}{l} 10x - 4y = 6 \\ -10x + 5y = 0 \end{array} & \begin{array}{l} y = 6 \end{array} \end{array}$$

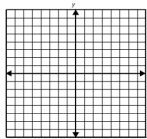
$$2) \begin{cases} x + y = -12 \\ 2x - 3y = 6 \end{cases} \quad (-6, -6)$$

$$\begin{array}{r|l} \begin{array}{l} x + y = -12 \\ 3x + 3y = -36 \end{array} & \begin{array}{l} -6 + y = -12 \\ y = -6 \end{array} \\ \hline \begin{array}{l} 2x - 3y = 6 \\ 5x = -30 \end{array} & \begin{array}{l} x = -6 \end{array} \end{array}$$

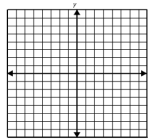
$$1) \begin{cases} 2x + 3y = 4 \\ 3x - 4y = 7 \end{cases} \quad \left(\frac{37}{17}, -\frac{2}{17}\right)$$

$$\begin{array}{r|l} \begin{array}{l} 2x + 3y = 4 \\ 8x + 12y = 16 \end{array} & \begin{array}{l} 2\left(\frac{37}{17}\right) + 3y = 4 \\ 17\left(\frac{74}{17} + 3y\right) = 4(17) \\ 74 + 51y = 68 \\ 51y = -6 \\ y = -\frac{6}{51} = -\frac{2}{17} \end{array} \\ \hline \begin{array}{l} 9x - 12y = 21 \\ 17x = 37 \end{array} & \begin{array}{l} x = \frac{37}{17} \end{array} \end{array}$$

7)  $\begin{cases} -2y < 4x + 2 \\ y > 2x + 1 \end{cases}$



8)  $\begin{cases} y \leq -2x + 4 \\ x > -3 \\ y \geq 1 \end{cases}$



Cumulative Questions:

9) Find the equation of the line through the points  $(-4, 7)$  and  $(-5, 2)$ .

Perform the following operations given  $f(x) = x^2 + 4$  and  $g(x) = 2x - 6$ .

10)  $f(x) - g(x) =$

11)  $(f \cdot g)(x) =$

12)  $f(g(x)) =$

13) Find the inverse of  $g(x)$ .

Perform the following operations given  $f(x) = x^2 + 4$  and  $g(x) = 2x - 6$ .

$$\begin{aligned} f(2x-6) &= (2x-6)^2 + 4 \\ &= (2x-6)(2x-6) + 4 \\ &= 4x^2 - 12x + 36 + 4 \\ &= 4x^2 - 12x + 40 \end{aligned}$$

12)  $f(g(x)) =$

$$\begin{aligned} g(x) &= 2x - 6 \\ y &= 2x - 6 \\ x &= \frac{y+6}{2} \\ 2y &= x + 6 \\ y &= \frac{x+6}{2} \end{aligned}$$

13) Find the inverse of  $g(x)$ .

$$g^{-1}(x) = \frac{x+6}{2}$$

Perform the following operations given  $f(x) = x^2 + 4$  and  $g(x) = 2x - 6$ .

10)  $f(x) - g(x) =$

11)  $(f \cdot g)(x) =$

$$\begin{aligned} (x^2 + 4) - (2x - 6) \\ x^2 + 4 - 2x + 6 \\ \boxed{x^2 - 2x + 10} \end{aligned}$$

$$\begin{aligned} (x^2 + 4)(2x - 6) \\ \boxed{2x^3 - 6x^2 + 8x - 24} \end{aligned}$$

9) Find the equation of the line through the points  $(-4, 7)$  and  $(-5, 2)$ .

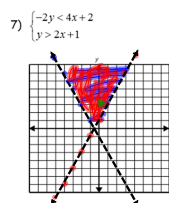
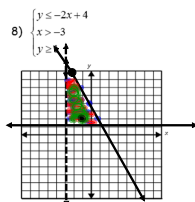
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{2 - 7}{-5 - (-4)} = \frac{-5}{-1} = 5$$

$$y - y_1 = m(x - x_1)$$

$$y - 7 = 5(x - (-4))$$

$$\begin{aligned} y - 7 &= 5x + 20 \\ +7 &+7 \\ \boxed{y} &= \boxed{5x + 27} \end{aligned}$$



$$\begin{aligned} -2y &< 4x + 2 \\ \frac{-2y}{-2} &< \frac{4x + 2}{-2} \\ y &> -2x - 1 \end{aligned}$$

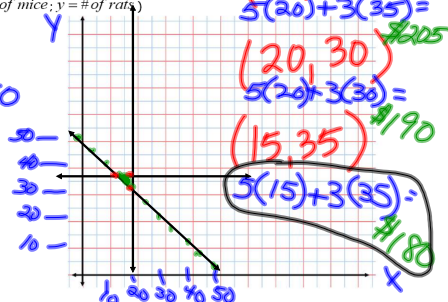
Solve the following linear programming problem (Use your graph provided, and make sure your answer is a **complete sentence**.)

14) A biologist needs at least 50 rodents for an experiment. She cannot use more than 20 mice or more than 35 rats. Each mouse costs \$5.00 and each rat costs \$3.00. How many of each rodent should she use in order to minimize the cost?

Constraints: ( $x$  = # of mice;  $y$  = # of rats)

$x + y \geq 50$   
 $x \leq 20$   
 $y \leq 35$

$$y \geq -x + 50$$



The biologist should use 15 mice and 35 rats.